

$$I = \frac{(2-3f)^2}{16} \frac{\sin^2 N\pi\zeta}{\sin^2 \pi\zeta} + \frac{3(2-f)^2}{16} \frac{\sin^2 N\pi(\zeta-\frac{1}{2})}{\sin^2 \pi(\zeta-\frac{1}{2})} + NE,$$

$$E = \frac{3}{8} f(1-f)(2-f) \left\{ \frac{1}{2-f(2-f)(1+\cos 2\pi\zeta)} \right\}$$

$$+ \frac{3}{2-f(2-f)(1-\cos 2\pi\zeta)}$$

where f is the fraction of 'twinned' two-layer sequences, which is related to β as $f=2\beta/(1+\beta)$.

The first and second terms of the equation for I give the sharp reflexions due to the above remarkable feature of the double fault; each of them is the Laue function having the principal maxima at $\zeta=0$ or $\frac{1}{2} \bmod 1$, but with a coefficient involving f . The two coefficients are plotted in Fig. 2 against f . The last term NE gives the diffuse reflexions due to the faults. As is seen in Fig. 3, the peaks of the function E become sharper and higher as f increases. Peak displacement does not occur in any case.

For $f=\beta=0$, I gives duly the diffraction from the starting h.c.p. crystal; the coefficients in the first and second terms become $\frac{1}{8}$ and $\frac{3}{8}$, respectively, and E vanishes. The crystal for $f=\beta=1$ is the twin, as a whole, of the starting crystal, which should give rise to the diffraction same as that of the starting crystal. For $f=\beta=1$, however, the two coefficients become $\frac{1}{16}$ and $\frac{3}{16}$, respectively, although E duly vanishes. This discrepancy is ascribed to the above assumption regarding N . When the higher terms which have been neglected on this assumption for obtaining I are taken into account, the same reflexions as those for $f=\beta=0$ can duly be obtained for $f=\beta=1$.

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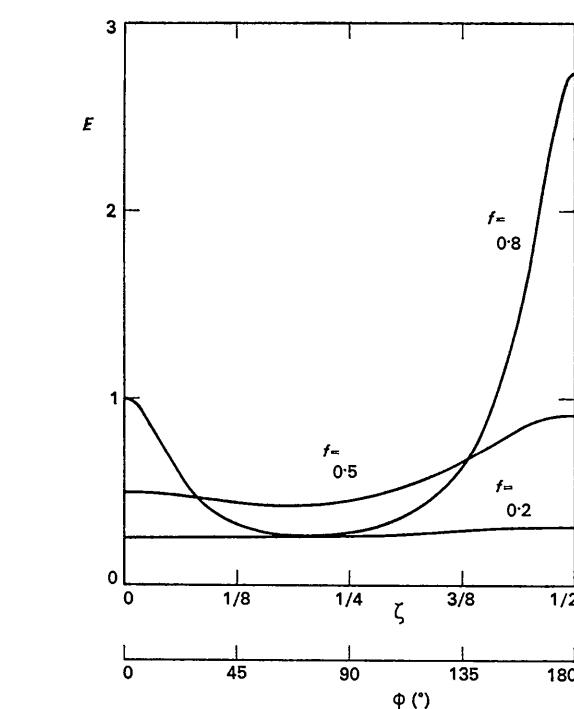


Fig. 3. The function E for various values of f . The curves are symmetric with respect to $\zeta=0$ and $\frac{1}{2}$. $\phi=360^\circ \times \zeta$.

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Phasenbeziehungen des tetragonalen Kristallsystems. Von ERNST SCHULTZE-RHONHOF, Anorganisch-Chemisches Institut der Universität, 53 Bonn, Meckenheimer Allee 168, Deutschland

(Eingegangen am 28. Mai 1968)

Attention is drawn to phase relations of reflexions in tetragonal space groups missing from *International Tables for X-ray Crystallography*.

Im tetragonalen System kann man einer Netzebene (hkl) weitere 15 Ebenen zuordnen, deren Indices sich aus den Indices (hkl) durch Anwendung einer Gruppe von Operationen erzeugen lassen. Diese Operationen sind:

(a) Vorzeichenänderung von h , k und l , entsprechend Spiegelungen an den Ebenen $0kl$, $h0l$ und $hk0$ im reziproken Gitter, und

(b) Vertauschen der Indices h und k , entsprechend einer Spiegelung an der Ebene $hh\bar{l}$.

Die Strukturamplituden $|F(hkl)|$ und Phasen $\alpha(hkl)$ dieser 16 Netzebenen sind durch Gesetzmäßigkeiten verknüpft, die bisher nur für diejenigen Flächen tabelliert sind, die durch Anwendung der Untergruppe (a) auseinander hervorgehen (*International Tables for X-ray Crystallography*, 1952). Diese Arbeit, die in Reihenfolge und Aufstellung der einzelnen Raumgruppen den *International Tables* (1952)

folgt, gibt eine Tabelle der fehlenden Zusammenhänge.* Die Formeln wurden für alle möglichen Fälle analytisch berechnet und davon unabhängig auf der IBM 7090 des Rheinisch-Westfälischen Institutes für Instrumentelle Mathematik, Bonn, nachgeprüft.

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* Editorial note: The Table is omitted from this Short Communication because the information which it contains will be included in a complete list of corrections for Vol. I which is being prepared by the Commission on *International Tables*. It is proposed to publish the list in the near future.